

CTOD: Crack tip opening displacement

T.L. Anderson. Chap.3 Elastic-plastic Fracture Mechanics

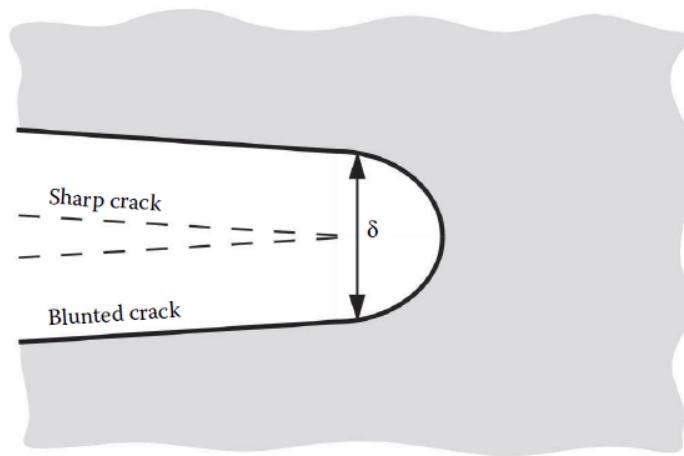


FIGURE 3.1

Crack tip opening displacement (CTOD). An initially sharp crack blunts with plastic deformation, resulting in a finite displacement (δ) at the crack tip.

Wells, A.A., Unstable crack propagation in metals: Cleavage and fast fracture. *Proceedings of the Crack Propagation Symposium*, Vol. 1, Paper 84, Cranfield, UK, 1961.

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TABLE 2.2

Crack Tip Displacement Fields for Modes I and II (Linear Elastic, Isotropic Material)

	Mode I	Mode II
u_x	$\frac{K_I}{2\mu} \sqrt{\frac{r}{2\pi}} \cos\left(\frac{\theta}{2}\right) \left[\kappa - 1 + 2 \sin^2\left(\frac{\theta}{2}\right) \right]$	$\frac{K_{II}}{2\mu} \sqrt{\frac{r}{2\pi}} \sin\left(\frac{\theta}{2}\right) \left[\kappa + 1 + 2 \cos^2\left(\frac{\theta}{2}\right) \right]$
u_y	$\frac{K_I}{2\mu} \sqrt{\frac{r}{2\pi}} \sin\left(\frac{\theta}{2}\right) \left[\kappa + 1 - 2 \cos^2\left(\frac{\theta}{2}\right) \right]$	$-\frac{K_{II}}{2\mu} \sqrt{\frac{r}{2\pi}} \cos\left(\frac{\theta}{2}\right) \left[\kappa - 1 - 2 \sin^2\left(\frac{\theta}{2}\right) \right]$

Note: μ is the shear modulus; $\kappa = 3 - 4v$ (plane strain); $\kappa = (3 - v)/(1 + v)$ (plane stress).

In mode I:

$$u_y = \frac{K_I}{2\mu} \sqrt{\frac{r}{2\pi}} [\kappa + 1] \quad \text{at } \theta = \pi \quad \text{with } \kappa = 3 - 4v \text{ in PE and } \kappa = (3 - v)/(1 + v) \text{ in PS}$$

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CTOD using the Irwin estimation of the plastic zone size, r_y

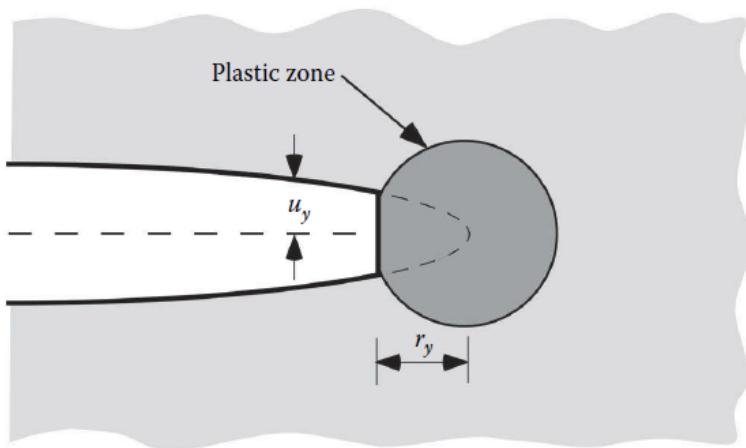


FIGURE 3.2

Estimation of CTOD from the displacement of the effective crack in the Irwin plastic zone correction.

$$\delta = 2u_y = \frac{4}{\pi} \frac{K_I^2}{\sigma_{YS}E} = \frac{4}{\pi} \frac{\mathcal{G}}{\sigma_{YS}}$$

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CTOD using the Yield strip model with a plastic zone size ρ

$$\rho = \frac{\pi^2 \sigma^2 a}{8 \sigma_{YS}^2} = \frac{\pi}{8} \left(\frac{K_I}{\sigma_{YS}} \right)^2$$

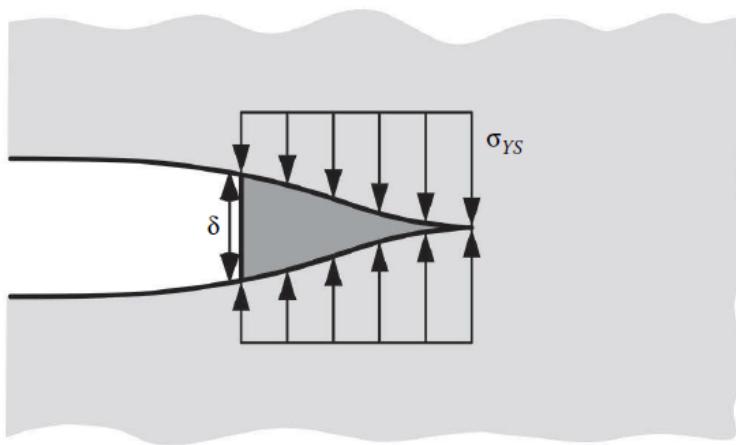


FIGURE 3.3
Estimation of CTOD from the strip yield model.

$$\delta = 2 \frac{G}{\sigma_{YS}} \text{ thus } G = \frac{1}{2} \delta \sigma_{YS} \left[\text{J/m}^2 \right] \text{ with } G, \text{ the energy release rate}$$

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CTOD can be measured on edge-cracked specimens loaded in 3 point bending

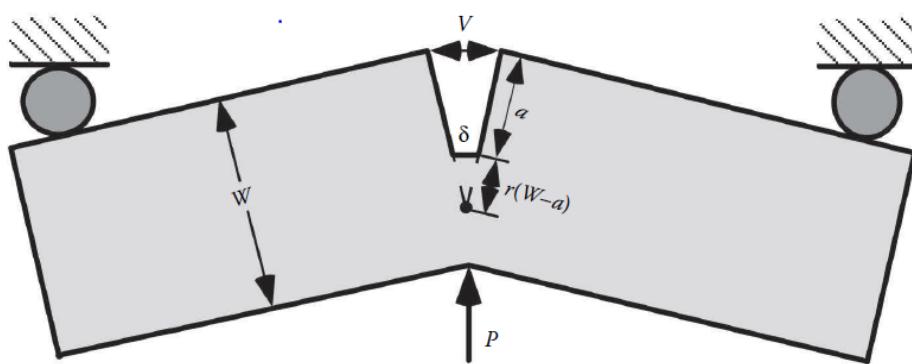


FIGURE 3.5

The hinge model for estimating CTOD from three-point bend specimens.

$$\frac{\delta}{r(W-a)} = \frac{V}{r(W-a) + a}$$

$$\delta = \frac{r(W-a)V}{r(W-a) + a}$$

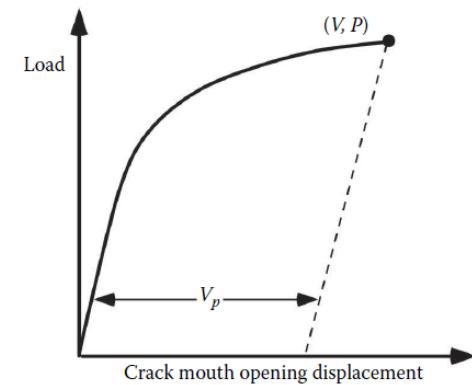


FIGURE 3.6

Determination of the plastic component of the crack mouth opening displacement.

$$V = V_{el} + V_{pl}$$

$$\delta = \delta_{el} + \delta_p = \frac{K_I^2}{m\sigma_{YS}E'} + \frac{r_p(W-a)V_p}{r_p(W-a) + a}$$

$$r_p = 0.44 \text{ (plastic rotational factor)}$$

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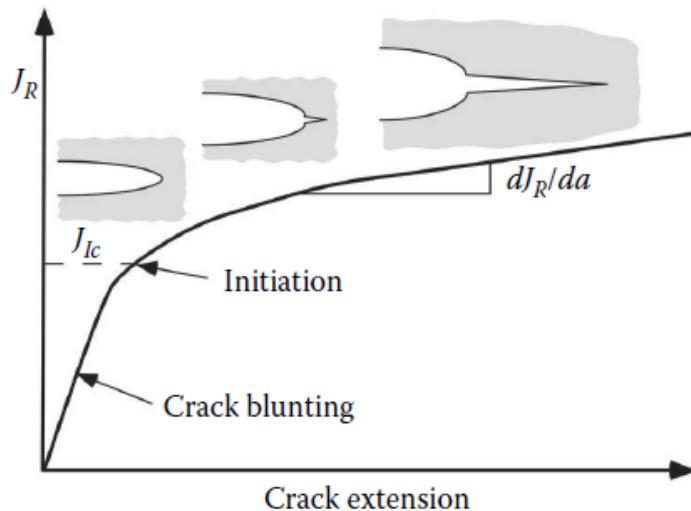


FIGURE 3.19

Schematic J resistance curve for a ductile material.

Typical J resistance curve for a ductile material. In the initial stages of deformation, the R curve is relatively steep; there is a small amount of apparent crack growth due to blunting. As J increases, the material at the crack tip fails locally and the crack advances further.

Fracture mechanics

Last class on May 26th

- Recap and Q&As

- Fracture mechanics, T.L. Anderson
- Available at EPFL library and online
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